

Parity dependence of Nuclear Level Density

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Abstract: The knowledge parity dependent nuclear level density $\rho(E, J, \pi)$ is very essential in low energy nuclear physics as it is used to evaluate nuclear cross-sections in nuclear reaction calculations. At low excitation energies, astrophysical reaction rates are sensitive to the parity distribution. However, the information of level density is confined to a rather small region of excitation energy, angular momentum and parity. Several theoretical studies have shown that at low energies there is a dominance of one type of parity and near the particle separation energy that parity ratio only approaches to an equal distribution. An accurate determination of nuclear level density and its dependence on mass number, excitation energy, angular momentum, parity, etc. is necessary for precise prediction of cross sections using the statistical models. In the present work, an absolute asymmetry parameter is used to determine the level density of negative as well as for positive parity states by using s- and p- wave (D_0 and D_1) neutron level spacing. The systematic are investigated from $23 < A < 238$ and compared to the pattern found in previous investigations. The present analysis also provides useful information on various resonance parameters at different nuclear mass regions with results that support the original conclusions.

Keywords: Parity; Thermal and statistical models; Level density

I. Introduction

Description of parity-violating processes and neutron-capture reactions are important requires parity and its statistical distribution. Level densities can have considerable parity reliant as is shown by analysis of experimental data [1] and theoretical studies [2-6]. Total and parity projected level densities were calculated by using Quantum Monte Carlo methods [7, 8]. The ratio of densities of negative and positive parity states in the neutron binding energy is usually assumed to be unity which is in accordance with some experimental results [1-5, 9, 10]. Calculations of Nakada and Alhassid [11] by employing projection method of Ref. [12] and SMMC representation of the partition function for a fixed parity clearly indicate strong parity dependence for small excitation energies. Systematic for parity distribution of nuclear level density near neutron separation energies have also been investigated by Singhal et al. [10]. Therefore, it is important to understand the dependence of nuclear level density on the key nuclear parameters like spin, parity, excitation energy etc.

According to Bethe's Fermi gas model, the nucleons were non-interacting and are proportional with the nuclear density function. In general, nuclear level density ρ can be

expressed as a function of various quantum numbers like excitation energy U , angular momentum J and parity π as;

$$\rho(U, J, \pi) = F_{\pi}(U) F_J(U, J) \rho(U)$$

Where,

$$\rho(U) = \frac{1}{12\sqrt{2}\sigma} \frac{e^{2\sqrt{aU}}}{a^{1/4}U^{5/4}}$$

And

$$F_J(U, J) = \frac{2J+1}{2\sigma^2} e^{-J(J+1)/2\sigma^2}$$

Here

- σ^2 = Spin cut-off parameter
- a = Nuclear level density parameter
- U = $S_n - \Delta$ = Excitation Energy
- Δ = Pairing energy due to odd even effect

As reported in the literature [1-5, 7, 8, 11-13], parity included nuclear level density function creates a large difference in the predicted theoretical cross sections. Ericson studied the parity asymmetry as a function of excitation energy. In the present study, we have determined the parity ratios at neutron binding energies for 110 nuclei between

²³Na and ²³⁸U by using microscopic theory. In order to take into account the energy dependence of parity distribution of nuclear level density, three parameters mainly absolute asymmetry parameter ($|\alpha|$), absolute asymmetry parameter per nucleon ($|\alpha|/A$) and nuclear temperature (T_N) with respect to excitation energy (U) and mass number (A) curves have been plotted. A systematic study of the behavior of the parity ratio, free parameter (β) and nuclear temperature (T_N) across a large mass region was also performed.

Rest of the paper is organized as follows, Section I contains the introduction of parity dependence of nuclear level density; with reference from the theoretical and experimental results. Section II contain the related work of nuclear level density calculations and their analysis, Section III describes results and discussion calculated through the data, their calculations and finally from their graphs, Section IV concludes research work with future directions.

II. Parity Ratio Analysis

A large fraction of the level density information currently available comes from neutron resonance analysis. At low energies, the neutron can only interact with the nucleus in an S state. As we move towards large excitation energies level density (ρ) approaches to the value of $1/2$. At low energies ρ is 1 for even-even nuclei. If a positive and negative parity orbit is nearly degenerate at the Fermi level than ρ can be near $1/2$ for odd A at low energy. If experiments have missed levels of a particular parity at a few MeV, the parity ratio will not approach $1/2$ as the energy increases. For heavy nuclei [14, 15], positive and negative parity states are expected to become equal already at low excitation energy to the order of a few MeV, while in lighter spherical nuclei stronger shell effects keep the ratio $\rho(\pi = +) / \rho(\pi = -)$ considerably different from unity over a wider energy range [16, 17].

Here we take the absolute asymmetry parameter (α) as;

$$\alpha = \frac{D_0}{D_0 + D_1} \dots(1)$$

where, D_0 & D_1 are the s - wave and p - wave level spacing obtained from Atlas of neutron resonances [18]. An important drawback for neutron resonance data is that almost all of the available information is for s -wave resonances; for the large majority of neutron resonance data obtained at low neutron energies, there is limited information on p -wave resonances. This is because most of the neutron resonance measurements are performed at such low neutron energies. Different parity ratio have been calculated for different spin of the target nuclei but the actual formula obtained for α is same as in eq.(1) for all the spins as

$$\alpha = \frac{3\rho_-}{3\rho_- + \rho_+} \text{ and } \frac{\rho_+}{\rho_-} = \frac{3D_1}{D_0} \text{ for } I^\pi = 0^+$$

$$\alpha = \frac{9\rho_-}{9\rho_- + 4\rho_+} \text{ and } \frac{\rho_+}{\rho_-} = \frac{9D_1}{4D_0} \text{ for } I^\pi = \frac{1}{2}^+$$

$$\alpha = \frac{2\rho_-}{2\rho_- + \rho_+} \text{ and } \frac{\rho_+}{\rho_-} = \frac{2D_1}{D_0} \text{ for } I^\pi = \frac{3}{2}^+, \frac{5}{2}^+, \frac{7}{2}^+ \text{ and } \frac{9}{2}^+$$

where, ρ_- & ρ_+ are the density of negative positive parity states. Value of α should be asymmetrically distributed about zero. From the available neutron resonance data for 110 nuclei in Atlas of Neutron Resonances [18] we obtain the best possible results. Many nuclear structure models have been employed and tested for the calculation of nuclear state densities at excitation energies corresponding to the neutron binding energy (of the order of 8 MeV for medium and heavy nuclei). This is because at those excitation energies an important experimental quantity can be related to the density of nuclear levels; the average spacing of s -wave neutron resonances $\langle D \rangle_{I=0}$. A large set of information on these quantities has been collected and compiled several times in the past. The data has been taken from Atlas of Neutron Resonances [18], and by using eq.(1) the values of absolute asymmetry parameter (i.e. parity ratio ($|\alpha|/A$), absolute asymmetry parameter per nucleon ($|\alpha|/A$) with error ($\Delta|\alpha|/A$), free parameter (β), nuclear temperature (T_N) for 110 nuclei of positive and negative parity states has been calculated and listed in Table1 given below.

Table1. Calculated absolute asymmetry parameter $|\alpha|$, asymmetry parameter per nucleon $|\alpha|/A$ with error $\Delta|\alpha|/A$, free parameter β and Nuclear temperature T_N values from s and p wave level spacings ($D_0, \Delta D_0, D_1, \Delta D_1$) for different nuclei.

Nucleus	A	I^π	$U = S_n - \Delta$ (MeV)	D_0 (keV)	ΔD_0 (keV)	D_1 (keV)	ΔD_1 (keV)	$ \alpha $	$ \alpha /A$	$\Delta \alpha /A$	$\beta(\text{MeV}^{-1})$	T_N
Na-11	23	3/2+	6.96	122	30	54	7	0.69	0.030	0.009	0.300	1.739
Al-13	27	5/2+	7.725	53	7	28.4	2.6	0.648	0.024	0.004	0.285	1.691
Si-14	28	0+	6.206	332	35	109	11	0.728	0.026	0.003	0.346	1.488
P-15	31	1/2+	7.937	54.9	10.4	21.5	2.2	0.713	0.023	0.005	0.280	1.600

S-16	32	0+	6.520	179	29	46.3	4.1	0.768	0.024	0.005	0.335	1.427
S-16	34	0+	4.928	111	40	47.5	4	0.68	0.020	0.009	0.463	1.203
Cl-17	35	3/2+	8.579	22.3	2.5	6.6	3.8	0.77	0.022	0.005	0.262	1.565
K-19	39	3/2+	7.8	19.5	3	5.6	0.5	0.741	0.019	0.004	0.294	1.414
Ar-18	40	0+	4.201	51.9	2.3	11.4	0.5	0.8	0.020	0.001	0.543	1.024
Ca-20	40	0+	6.465	45	4	16	1	0.72	0.018	0.002	0.361	1.273
Ti-22	46	0+	7.110	20	3	6.7	0.5	0.736	0.016	0.003	0.337	1.243
Ti-22	47	5/2-	11.626	1.64	0.13	0.47	0.06	0.752	0.016	0.001	0.205	1.572
Ti-22	48	0+	6.409	20.8	2.5	8.7	0.87	0.672	0.014	0.002	0.382	1.155
Ti-22	49	7/2-	10.939	4.52	0.31	1.5	0.2	0.735	0.015	0.001	0.222	1.494
Cr-24	50	0+	7.563	11.73	0.84	3.69	0.27	0.75	0.015	0.001	0.321	1.229
V-23	51	7/2-	7.311	3.95	0.27	1.7	0.14	0.663	0.013	0.001	0.340	1.197
Cr-24	52	0+	6.274	34.9	3.2	10.5	0.5	0.728	0.014	0.001	0.390	1.098
Cr-24	53	3/2-	9.719	5.96	0.47	3.06	0.2	0.636	0.012	0.001	0.260	1.354
Cr-24	54	0+	4.613	44.3	5.3	7.72	0.36	0.81	0.015	0.002	0.524	0.924
Fe-26	54	0+	7.665	15.5	1	4.75	0.15	0.756	0.014	0.001	0.322	1.191
Mn-25	55	5/2-	7.270	2.42	0.15	1.1	0.1	0.66	0.012	0.001	0.348	1.149
Fe-26	56	0+	6.042	22	1.7	8.21	0.48	0.728	0.013	0.001	0.416	1.038
Fe-26	57	1/2-	10.044	7.05	0.67	2.58	0.26	0.684	0.012	0.001	0.250	1.327
Fe-26	58	0+	5.005	21.6	2.6	5.03	0.3	0.754	0.013	0.002	0.495	0.928
Ni-28	58	0+	7.423	12.92	0.83	4.04	0.14	0.754	0.013	0.001	0.338	1.131
Co-27	59	7/2-	7.491	1.37	0.07	0.8	0.047	0.59	0.010	0.0007	0.348	1.126
Ni-28	60	0+	6.270	12.53	0.98	3.02	0.12	0.78	0.013	0.001	0.398	1.022
Cu-29	63	3/2-	7.916	0.722	0.047	0.404	0.022	0.73	0.010	0.0009	0.333	1.120
Ni-28	64	0+	4.598	21.1	2	9.2	0.6	0.64	0.010	0.001	0.566	0.847
Zn-30	64	0+	6.479	2.94	0.13	1	0.05	0.704	0.011	0.0007	0.396	1.006
Cu-29	65	3/2-	7.066	1.52	0.1	0.628	0.039	0.65	0.010	0.001	0.368	1.042
Zn-30	66	0+	5.574	4.7	0.4	0.84	0.05	0.792	0.012	0.001	0.452	0.919
Zn-30	67	5/2-	10.198	0.367	0.019	0.123	0.005	0.737	0.011	0.0007	0.254	1.233
Zn-30	68	0+	5.026	3.785	0.19	1.267	0.037	0.748	0.011	0.0007	0.516	0.859
Ga-31	69	3/2-	7.653	0.316	0.041	0.123	0.06	0.69	0.010	0.002	0.343	1.053
Zn-30	70	0+	4.399	3.51	0.17	1.36	0.04	0.7	0.010	0.0006	0.598	0.792
Ga-31	71	3/2-	6.520	0.326	0.041	0.113	0.011	0.71	0.010	0.001	0.402	0.958
As-33	75	3/2-	7.328	0.093	0.006	0.054	0.003	0.6	0.008	0.0007	0.372	0.988
Se-34	76	0+	6.042	0.505	0.065	0.236	0.033	0.608	0.008	0.001	0.447	0.891
Se-34	77	1/2-	10.497	0.121	0.011	0.054	0.005	0.616	0.008	0.001	0.257	1.167
Se-34	78	0+	5.604	1.48	0.2	0.515	0.35	0.702	0.009	0.002	0.476	0.847
Br-35	79	3/2-	7.892	0.053	0.002	0.032	0.003	0.553	0.007	0.0006	0.350	0.999
Se-34	80	0+	5.359	3.5	1.5	2.2	1.6	0.56	0.007	0.005	0.518	0.818
Br-35	81	3/2-	7.593	0.145	0.008	0.059	0.004	0.648	0.008	0.0007	0.357	0.968
Kr-36	84	0+	5.811	4.04	0.45	1.65	0.165	0.672	0.008	0.001	0.469	0.831
Rb-37	85	5/2-	8.651	0.172	0.008	0.063	0.002	0.68	0.008	0.0005	0.314	1.008
Kr-36	86	0+	4.221	25.5	2.2	8.39	0.4	0.688	0.008	0.001	0.642	0.700

Sr-38	87	9/2+	11.113	0.44	0.07	0.156	0.011	0.696	0.008	0.001	0.245	1.130
Sr-38	88	0+	5.079	25	5	8.7	1.1	0.704	0.008	0.002	0.537	0.759
Y-39	89	1/2-	6.857	4.79	0.3	1.423	0.043	0.712	0.008	0.0007	0.396	0.877
Zr-40	90	0+	5.930	6.89	0.53	3.55	0.2	0.63	0.007	0.0007	0.472	0.811
Zr-40	91	5/2+	8.635	0.536	0.048	0.251	0.014	0.637	0.007	0.0008	0.323	0.974
Zr-40	92	0+	5.483	3.8	0.51	1.535	0.09	0.644	0.007	0.001	0.506	0.772
Mo-42	92	0+	6.818	2.8	0.485	0.78	0.067	0.736	0.008	0.001	0.400	0.860
Zr-40	93	5/2+	7.228	0.302	0.075	0.149	0.015	0.651	0.007	0.002	0.388	0.881
Nb-41	93	9/2+	8.221	0.084	0.004	0.042	0.001	0.651	0.007	0.0005	0.342	0.940
Zr-40	94	0+	5.224	4	0.73	1.236	0.074	0.752	0.008	0.001	0.526	0.745
Mo-42	94	0+	6.131	1.694	0.39	0.508	0.047	0.752	0.008	0.002	0.448	0.807
Mo-42	95	5/2+	9.154	0.081	0.014	0.037	0.004	0.665	0.007	0.001	0.307	0.981
Zr-40	96	0+	4.350	13	4	4.5	1	0.672	0.007	0.003	0.637	0.673
Mo-42	96	0+	5.596	1.17	0.28	0.324	0.025	0.768	0.008	0.002	0.491	0.763
Mo-42	97	5/2+	8.643	0.046	0.005	0.021	0.001	0.679	0.007	0.001	0.326	0.943
Mo-42	98	0+	4.712	0.97	0.2	0.286	0.014	0.686	0.007	0.002	0.586	0.693
Tc-43	99	9/2+	6.764	0.012	0.0005	0.006	0.0003	0.594	0.006	0.0003	0.422	0.826
Mo-42	100	0+	4.198	0.617	0.07	0.236	0.021	0.7	0.007	0.001	0.669	0.647
Ru-44	100	0+	5.602	0.447	0.044	0.115	0.007	0.7	0.007	0.001	0.492	0.748
Ru-44	102	0+	5.043	0.375	0.07	0.125	0.007	0.714	0.007	0.001	0.555	0.703
Rh-45	103	1/2-	6.998	0.028	0.001	0.013	0.0007	0.618	0.006	0.0004	0.408	0.824
Ru-44	104	0+	4.733	0.482	0.055	0.106	0.012	0.728	0.007	0.001	0.584	0.674
Pd-46	104	0+	5.917	0.194	0.03	0.081	0.007	0.624	0.006	0.001	0.480	0.754
Pd-46	105	5/2+	9.561	0.010	0.0005	0.005	0.0007	0.63	0.006	0.0005	0.299	0.954
Pd-46	106	0+	5.370	0.174	0.025	0.061	0.004	0.636	0.006	0.001	0.526	0.711
Cd-48	106	0+	6.758	0.135	0.035	0.052	0.006	0.636	0.006	0.002	0.420	0.798
Ag-47	107	1/2-	7.271	0.014	0.0005	0.008	0.0002	0.535	0.005	0.0003	0.399	0.824
Pd-46	108	0+	4.999	0.135	0.024	0.045	0.003	0.648	0.006	0.001	0.566	0.680
Cd-48	108	0+	6.172	0.12	0.03	0.048	0.003	0.648	0.006	0.002	0.462	0.755
Ag-47	109	1/2-	6.809	0.015	0.0006	0.006	0.0005	0.654	0.006	0.0004	0.422	0.790
Pd-46	110	0+	4.581	0.334	0.043	0.106	0.009	0.66	0.006	0.001	0.618	0.645
Cd-48	110	0+	5.831	0.247	0.02	0.08	0.005	0.66	0.006	0.0007	0.486	0.728
Cd-48	111	1/2+	9.394	0.026	0.002	0.014	0.0009	0.555	0.005	0.0006	0.309	0.919
Cd-48	112	0+	5.406	0.174	0.011	0.059	0.002	0.672	0.006	0.0005	0.527	0.694
Cd-48	113	1/2+	9.043	0.024	0.0006	0.011	0.0006	0.678	0.006	0.0002	0.319	0.894
Cd-48	114	0+	5.017	0.233	0.03	0.087	0.008	0.684	0.006	0.001	0.572	0.663
In-49	115	9/2+	6.785	0.009	0.0004	0.005	0.0002	0.575	0.005	0.0003	0.436	0.768
Cd-48	116	0+	4.662	0.704	0.27	0.215	0.02	0.696	0.006	0.003	0.612	0.634
Sn-50	116	0+	5.828	0.507	0.06	0.155	0.006	0.696	0.006	0.001	0.489	0.708
Sn-50	117	1/2+	9.327	0.061	0.007	0.031	0.003	0.585	0.005	0.0008	0.314	0.892
Sn-50	118	0+	5.379	0.7	0.15	0.32	0.04	0.59	0.005	0.001	0.542	0.675
Sn-50	120	0+	5.074	1.485	0.13	0.378	0.013	0.72	0.006	0.0007	0.562	0.650
Sn-50	122	0+	4.859	2.965	0.145	1.03	0.03	0.732	0.006	0.0003	0.595	0.633

Te-52	122	0+	5.842	0.146	0.014	0.063	0.003	0.61	0.005	0.0007	0.500	0.692
Sn-50	124	0+	4.655	6.25	0.65	1.631	0.07	0.744	0.006	0.0008	0.616	0.612
Te-52	124	0+	5.491	0.22	0.03	0.127	0.012	0.62	0.005	0.0009	0.543	0.665
Te-52	126	0+	5.218	0.64	0.17	0.247	0.022	0.63	0.005	0.001	0.560	0.643
Te-52	128	0+	5.021	1.51	0.375	0.6	0.077	0.64	0.005	0.001	0.585	0.626
Ba-56	134	0+	5.936	0.36	0.048	0.12	0.009	0.67	0.005	0.0009	0.494	0.665
Ba-56	136	0+	5.877	1.52	0.225	0.442	0.029	0.68	0.005	0.001	0.498	0.657
Ba-56	138	0+	3.701	18.7	2.9	6.76	0.67	0.69	0.005	0.001	0.800	0.517
Ce-58	140	0+	4.413	3.73	0.47	1.55	0.11	0.7	0.005	0.0008	0.677	0.561
Nd-60	142	0+	5.116	1.035	0.135	0.39	0.033	0.71	0.005	0.0008	0.582	0.600
Nd-60	143	7/2-	7.817	0.037	0.002	0.021	0.004	0.572	0.004	0.0005	0.390	0.739
Nd-60	144	0+	4.755	0.45	0.005	0.202	0.014	0.576	0.004	0.0001	0.634	0.574
Sm-62	144	0+	5.757	0.77	0.045	0.265	0.022	0.72	0.005	0.0004	0.517	0.632
Tl-81	203	1/2+	6.656	0.552	0.074	0.2	0.018	0.609	0.003	0.0006	0.474	0.572
Pb-82	204	0+	5.891	2.172	0.096	0.69	0.055	0.612	0.003	0.0002	0.533	0.537
Tl-81	205	1/2+	6.504	2.2	0.3	1.14	0.08	0.615	0.003	0.0005	0.494	0.563
Pb-82	206	0+	5.901	37.1	5.5	4.78	0.21	0.824	0.004	0.0008	0.520	0.535
Pb-82	207	1/2-	7.367	30	4	4.03	0.29	0.828	0.004	0.0007	0.417	0.596
Bi-83	209	9/2-	4.604	4.54	0.39	1.11	0.09	0.627	0.003	0.0004	0.678	0.469
U-92	238	0+	4.028	0.020	0.0007	0.007	0.0002	0.714	0.003	0.0001	0.803	0.411

III. Results and discussion:

A. Parity dependence of level densities

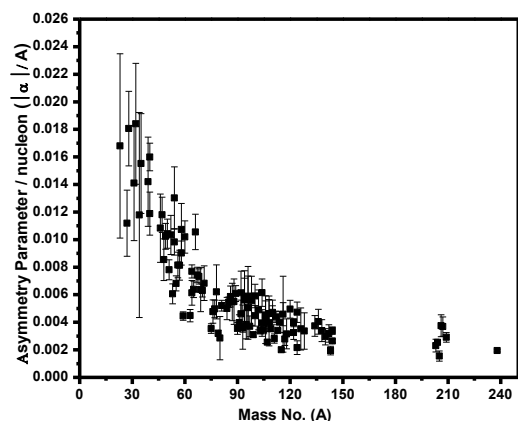


Fig1. Asymmetry parameter per nucleon ($|\alpha|/A$) vs Mass number (A)

From the analysis, it has been obvious that absolute asymmetry parameter per nucleon ($|\alpha|/A$) of compound nuclides decreases with the increase of mass number A and this behavior of ($|\alpha|/A$) is due to the fact that when mass number A increases; there is a redistribution of the positive

and negative parities states equally. Shell model Monte Carlo calculations [13, 14] in the nuclear $1f-2p$ shell also predict a significant parity dependence of the level density for some nuclides. The asymmetry values given by Mengoni [2] are comparable for some nuclei at low excitation energies. Values of $\rho-\rho+$ by Allhasid [19] for Fe-56, Ni-60 and Zn-68 and Uhrenholt [20] for Ni and Sr isotopes also somehow match to the value obtained by us. The ($|\alpha|/A$) obtained from high resolution neutron resonance data by Singhal et al [10] are in agreement with our calculated values in Fig. 1. The ($|\alpha|/A$) values for Ni, Sn and Sr and some of its isotopes calculated by Mocolj [21] is in conformity with our values. Al-Quraishi [22] also calculates the parity ratio for high as well as for low excitation energy at neutron excitation energies for the nuclides on stability line which leads to equipartition of parity levels quickly at higher excitation energies. U. Agvaanluvsan [23] also determines the parity dependence of nuclear level density for different spin-parity combinations by using asymmetry parameter in high resolution proton resonance data.

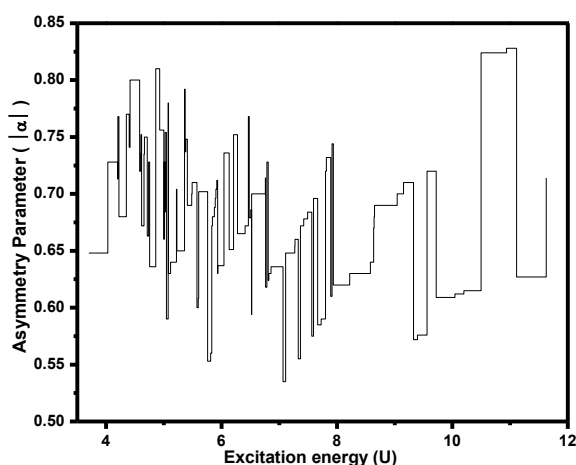


Fig2. Asymmetry parameter ($|\alpha|$) vs. Excitation energy (U)

In fig2 we determine the variation of absolute asymmetry parameter ($|\alpha|$) with excitation energy (U) and it is clear from the figure that there is a variation for positive and negative parity states but as we take the magnitude of the parameter (i.e. $|\alpha|$) that's why all variations have to be constructed on the positive side only. All the oscillations obtained between 0.5 to 0.85 i.e. close to 0.5 and 1 for all nuclei. This confirms the equiparity distribution among all the nuclei undertaken. Normally, one makes a assumption of parity equilibration as $\rho_+(E) = \rho_-(E) = \frac{1}{2} \rho(E)$ at all excitation energies. This is definitely not true at very low excitations. Parity ratios are only found to equilibrate up to 10 MeV of excitation energy. However, the recent analyses [10, 24] of the experimental data indicate that equilibration is not reached even up to moderately high excitations. Allhasid [8], Rauscher [25], Mengoni [2] investigate the effect of parity distribution of excited levels on the neutron capture reactions. Positive and negative parity dominated regions in the level density has been discovered by Cerf [4] who studied the parity distribution of excited nuclear levels.

B. Free parameter (β) and Nuclear temperature (T_N)

Now consider the energy dependence of absolute asymmetry parameter per nucleon ($|\alpha|/A$) for the available data on neutron separation energies, we introduce a simple energy depend function as;

$$\frac{|\alpha|}{A} = 1 - \tanh \beta U$$

In terms of nuclear temperature T_N ,

$$\beta = \frac{\tanh^{-1}\left(1 - \frac{|\alpha|}{A}\right)}{aT_N^2} \quad \text{where, } \beta \text{ is the free parameter.}$$

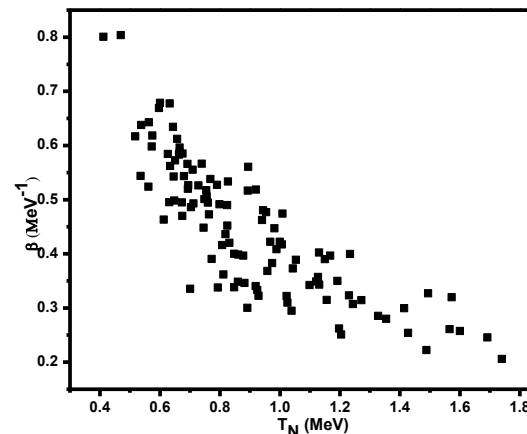


Fig3. Free Parameter (β) vs. Nuclear Temperature (T_N)

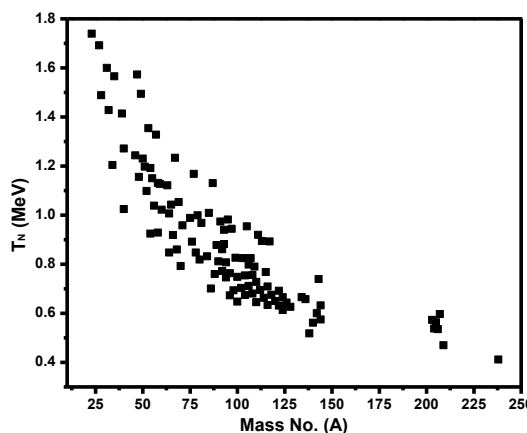


Fig4. Nuclear temperature (T_N) vs. mass number (A)

At low excitation energies, with increasing nuclear temperature T_N pairing interactions occurs in nuclear systems, leading to nucleon pairs in the ground state. The breaking of such pairs requires additional energy. Hence, at lower values of $T_N=1/\beta$ the Fermi-Dirac distribution will not be able to describe the occupation properly. At high T_N the microscopic distributions are well described by Fermi-Dirac statistics but for lower T_N deviations start to appear. Free parameter (β) as a function of nuclear temperature (T_N) is shown in Fig3 signifying that β decreases with the increase of T_N and supports the fact of equilibrium of parities at high excitations. With increase in mass number the nuclear

temperature (T_N) decreases as shown in Fig4, which was supported by the values obtained by Gilbert et al. [26] and Kawano et al. [27].

IV. Conclusions:

Nuclear level density is important for a variety of pure and applied nuclear physics. In this work, we have measured asymmetry parameter ($|\alpha|$), asymmetry parameter per nucleon ($|\alpha|/A$), free parameter (β), nuclear temperature (T_N) etc. for negative and positive parity states nuclei. A parity dependent formula has been developed to calculate the level spacing which further applied on both nuclei, giving an overall good agreement with the experimental data. From the model, the parity asymmetry can also be extracted. We have presented a simple method in the framework of the statistical Hauser-Feshbach theory to account for a full parity dependence including nonuniformly distributed parities in the nuclear level density of the compound nucleus. Further systematic study in this direction is also needed as less information is available on that.

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