Research Article

Simulation and Optical Absorption Analysis of Cr3+ doped Single Crystals of Potassium Magnesium Sulfate Chloride (Kainite)

Maroj Bharati¹ [,](http://orcid.org/0009-0007-8219-0993) Vikram Singh² [,](http://orcid.org/%200000-0003-3813-586X) Ram Kripal3[*](http://orcid.org/%200000-0002-3483-8704)

^{1,}Dept. of Physics, Nehru Gram Bharti (DU), Jamunipur, Prayagraj, India ³EPR Laboratory, Department of Physics, University of Allahabad, Prayagraj, India

**Corresponding Author: ram_kripal2001@rediffmail.com*

Received: 14/Aug/ 2024; **Accepted**: 16/Sept/2024; **Published**: 31/Oct/2024

Abstract— The zero field and crystal field splitting parameters for single crystals of Potassium Magnesium Sulphate Chloride (Kainite), KMgCST (KMgClSO₄.3H₂O) doped with Cr^{3+} ions are ascertained utilizing superposition model. For computation, the proper positions of the Cr^{3+} ions in the distorted KMgCST are considered. The zero field splitting parameters that are computed using local distortion closely match the values observed in experiments. The optical energy values for Cr^{3+} in KMgCST are estimated using the Crystal Field Analysis Program and crystal field parameters. The results show that a Cr^{3+} ion replaces one Mg^{2+} ion in KMgCST single crystals.

Keywords— Cr³⁺ ions in KMgCST; Crystal field; Optical spectroscopy; Superposition model; Zero-field splitting; EPR.

1. Introduction

The local symmetry of transition ions in crystals is investigated using the electron paramagnetic resonance (EPR) technique. The EPR of Cr^{3+} ion intoxicated into different crystals yields rich information about the parameters for zero field splitting (ZFS) and crystal fields (CF) [1-5]. When monovalent ions are substituted with divalent or trivalent impurities, it is crucial to compensate for the charge imbalance. Positive ion vacancies provide the charge compensation in systems where monovalent ions are replaced by divalent or trivalent impurities [6, 7]. The crystal's optical characteristics are influenced by doped impurities that result in slight structural changes. Superposition Model (SPM) is primarily used to determine ZFS and CF parameters theoretically [8–10].

Kainite, a mineral, having chemical formula KMgClSO4·3H2O is widely used in fertilizer industry [11]. It also falls under the category of mineral salts, which include antigorite and zeolites [12, 13], and are employed as catalysts in a variety of chemical processes.

EPR investigation for Cr^{3+} ions in KMgCST was carried out and spin Hamiltonian parameters estimated [14]. Mg^{2+} ions have an ionic radius of 0.072 nm, marginally greater than Cr^{3+} ions (0.0615 nm). As a result, as mentioned in [14], Cr^{3+} ions take the place of Mg^{2+} ions.

The altered crystallographic axes (a, b, and c*) and the laboratory axes (x, y, and z) are selected in parallel. The symmetry adopted axes (magnetic axes) are represented by (X, Y, Z). The crystallographic *a* axis is found to correspond with the g and D tensors of $Cr³⁺$ ions' principal Z axis. This investigation presents the CF and ZFS parameters for Cr^{3+} ions in KMgCST single crystal as analyzed by the superposition model (SPM). The objective is to examine the ZFS parameters, CF parameters, and lattice distortion for the $Cr³⁺$ ions in KMgCST at octahedral sites. The Crystal Field Analysis (CFA) computer program and CF parameters are used to estimate the optical energy values for Cr^{3+} ions in KMgCST. In subsequent research, CF and ZFS parameters assessed could be helpful in locating crystals for a variety of academic and commercial uses.

The purpose of the study and its subject introduction were covered in this section. The following is the arrangement of the paper's remaining sections. The related work for the SPM analysis is given in Section 2. The techniques for determining the ZFS and CF parameters are explained in Section 3. The procedure is given in Section 4. Section 5 presents the results and discussion. The study's conclusion and future scope are covered in section 6.

2. Related Work

As mentioned in [1-10], the SPM analysis was performed for a number of ion-host systems. $Z = 16$ and space group C2/m,

kainite (KMgClSO₄.3H₂O, KMgCST) crystallizes in a monoclinic system. β = 94◦ 55', *a* = 19.72 Å, *b* = 16.23 Å, *c* = 9.53 Å are the cell parameters [15]. Four chains make up a lattice along the Mg $(H_2O)_2-(SO_4)_2-(H_2O)_2-Mg$ $(H_2O)_2 (SO_4)_2$ — b-axis, the mirror plane contains the SO_4 tetrahedra. The chains are dispersed throughout the cell's (0 1 0) crosssection. The chains are held vertically together by K^+ and Cl ions. The asymmetric portion of the unit cell contains two magnesium atoms. Fig. 1 shows the KMgCST crystal structure and the symmetry adopted axis system (SAAS).

The symmetry adopted axes (SAA) or local site symmetry axes are the directions of mutually perpendicular metal-ligand bonds. The Z axis of SAAS is the metal-ligand bond Mg-O (crystal a-axis), and for center I, the other two axes (X, Y) are perpendicular to it (Fig. 1). This suggests that in the KMgCST crystal, Cr^{3+} takes the place of Mg^{2+} with symmetry roughly orthorhombic. The ionic radius of Mg^{2+} ions is 0.072 nm, while that of Cr^{3+} ions is 0.0615 nm, suggesting that Mg^{2+} ions' positions can be slightly distorted by \overline{Cr}^{3+} ions.

3. Theory/Calculation

In crystals, the energy states of Cr^{3+} ions are determined utilizing the spin Hamiltonian [16, 17, 18]:

$$
\mathcal{H}_{\text{ZFS}} = \mu_B B. g.S + \sum B_k^q O_k^q = \mu_B B. g.S + \sum f_k b_k^q O_k^q,
$$
\n(1)

where spectroscopic splitting factor, Bohr magneton and steady magnetic field are represented by g, μ_B and B, respectively. $O_k^q(S_x, S_y, S_z)$ represent the extended Stevens operators (ESO) and S stands for the effective spin operator [19, 20]; the ZFS parameters, $f_k = 1/3$ and 1/60 the scaling factors for $k = 2$ and 4, respectively are given by B_k^q and b_k^q . For orthorhombic symmetry of the Cr³⁺ ion (S = 3/2), the estimated ZFS terms in (1) are as given below [21, 22]:

$$
B_2^0O_2^0 + B_2^2O_2^2 = \frac{1}{3}b_2^0O_2^0 + \frac{1}{3}b_2^2O_2^2
$$

= $D(S_z^2 - \frac{1}{3}S(S+1)) + E(S_x^2 - S_y^2)$ (2)

 B_k^q , b_k^q and the traditional ZFS parameters D, E have relations as:

$$
b_2^0 = D = 3 B_2^0, \ b_2^2 = 3E = 3 B_2^2
$$
\n(3)

Using SPM [21-22], in ESO notation, the ZFS parameters in any symmetry are found as:

$$
b_k^q = \sum_i \overline{b}_k (R_0) \left(\frac{R_0}{R_i}\right)^{t_k} K_k^q \left(\theta_i, \varphi_i\right), \tag{4}
$$

where the spherical polar coordinates of i-th ligand are represented by $(R_i, \theta_i, \varphi_i)$. The k-th rank ZFS contribution from a ligand at the distance R_i is given by the intrinsic parameters \overline{b}_k and the geometrical information is provided by the coordination factors K_k^q . In ESO notation [23] K_k^q r $k = 1$ to 6 are presented in [24] (Appendix A1). Eq. (4) yi the nal ZFS paraneters, D and E, in

terms of the intrinsic parameters *bk* \overline{a} r-law exponents

$$
t_k
$$
 and the reference distance R₀, as given below [24, 25-27]:

$$
b_2^0 = D = \frac{\overline{b}_2(R_0)}{2} \left[\left(\frac{R_0}{R_i} \right)^{t_2} \sum_i (3 \cos^2 \theta_i - 1) \right] (5)
$$

$$
b_2^2 = 3E
$$

= $\frac{b_2^2}{3} = \frac{\overline{b}_2(R_0)}{2} \left[\left(\frac{R_0}{R_i} \right)^{t_2} \sum_i \sin^2 \theta_i \cos 2\varphi_i \right]$

4. Experimental Method/Procedure/Design

Table 1 presents the Cr^{3+} ion position and ligands' spherical polar coordinates for center I in KMgCST [15]. These specifics are employed for Cr^{3+} ions in KMgCST ZFS and CF computations.

Table 1. The Cr^{3+} ion's fractional coordinates and ligands' (center I) spherical polar co-ordinates (R, θ, ф) in a single KMgCST crystal. __

Cr^{3+} Position	Ligands		Spherical polar co-ordinates of ligands			
		RÅ	θ^0	ϕ^0		
ND: Substitutional	O1	9.4911	23.23	20.40		
(0.0000, 0.0000, 0.0000)	Ω Ow1	5.9749 2.1728	48.65 15.50	72.31 1.18		
	$\rm{Ow2}$	10.6079	49.75	87.31		
	Qw3	7.7182	9.74	33.67		
	Ow4	6.0005	76.52	84.99		
WD: substitutional Centre I O1		9.5972	24.41	-30.43		
$(0.2185, 0.1264, -0.00182)$	O ₂	5.6194	45.13	-38.53		
	Qw1	4.7197	63.43	30.02		
	\rm_{OW2}	10.1996	47.64	-57.06		
	Qw3	6.2761	7.57	-82.22		
	Ow4	5.6195	75.40	-44.80		

 $WD = With distortion, ND = No distortion.$

 $Cr³⁺$ ion in KMgCST is expected to be substituted at both the interstitial site and the Mg^{2+} ion site having comparable ligands environment. The Cr^{3+} ion has orthorhombic local

symmetry. Using $t_2 = -0.12$, $\bar{b}_2(R_0) = 2.34$ cm⁻¹ [28] and Cr^{3+} ion octahedral coordination with Cr^{3+} -O²⁻ bond in

LiNbO3, b_2^0 and b_2^2 were determined. The current study uses

 $t_2 = -0.96$ and $\bar{b}_2(R_0) = 2.34$ cm⁻¹ for center I to estimate the

 b_K^q because with oxygen acting as a ligand, the Cr³⁺ ion in KMgCST exhibits distorted octahedral coordination (Fig. 1). Equation (5) is used to obtain the ZFS parameters.

5. Results and Discussion

Equation (5) yields the traditional parameters of ZFS, D and E for the Cr^{3+} ion in KMgCST single crystal. The reference distance $R_0 = 0.200$ nm is used [29] to get the parameters of ZFS, $|D| = 930.9 \times 10^{-4}$ cm⁻¹ and $|E| = 797.3 \times 10^{-4}$ cm⁻¹ for center I. For symmetry that is orthorhombic, b_2^2/b_2^0 2 b_2^2/b_2^0 should be in the range 0 and 1 [30]. In the current computation, $|b_2^2|/|b_2^0|$ 2 b_2^2 | / | b_2^0 | = 2.569 and |E| / |D| = 0.856 for center I. It is found that the computed values of |D| and |E| do

not agree with the experimental ones and $|b_2^2|/|b_2^0|$ \overline{c} $b_2^2 \mid / \mid b_2^0 \mid$ also does not fall in the given range [30]. Therefore, with above t_2 and reference distance R_0 , the ZFS parameters $|D|$ and $|E|$ are computed for Cr^{3+} at the Mg^{2+} site with distortion having position Mg^{2+} (0.2185, 0.1264, -0.00182) for center I. The local surrounding about Cr^{3+} ion is shown in Fig. 2. The traditional ZFS parameters established now are |*D*| = 975.5×10^{-4} cm⁻¹, $|\vec{E}| = 57.2 \times 10^{-4}$ cm⁻¹ for center I, which match fairly well with the values of the experiment. The ratio $|b_2^2|/|b_2^0|$ 2 b_2^2 | / | b_2^0 | = 0.176 and |*E*| / |*D*| = 0.058 for center I lie in the specified range [31]. Further, with above t_2 and reference distance R_0 , the ZFS parameters $|D|$ and $|E|$ are computed for $Cr³⁺$ ion at the interstitial site but the values established differ much from the experimental ones. Due to this reason, these results are not presented here.

Fig. 2. Graphical depiction of local surrounding of $Cr³⁺$ ion (after distortion positions shown by dotted circles).

Table 2 displays the Cr^{3+} ion's ZFS parameters in KMgCST, both calculated and experimental. It is noted that the ZFS parameters |D| and |E| are in good agreement with the values obtained from the experiment [14] when the distortion is incorporated into calculation.

Table 2. ZFS parameters of Cr^{3+} in a single crystal of KMgCST for center I, along with reference distance, calculated and experimental.

	$ZFS (10^{-4}cm^{-1})$		Calculated parameters of ZFS (cm ⁻¹)	Traditional	parameters of
Site E	$R_0^{\text{Å}}$ E / D	$ b_{2}^{0} $		$ b_2^2 $ $ b_2^2 / b_2^0 $	D
ND 797.3	2.00 0.856	0.09309	0.23919	2.569	930.9
Center I WD 57.2	2.00 0.058	0.09755	0.01717	0.176	975.5
		975.5°	57.1° 0.058		

 $WD = With distortion, ND = No distortion, e = experimental.$

The transition metal ion CF energy states in crystals [31–34] may be found using Wybourne operators as given below [16, 35, 36]:

$$
\mathcal{H}_{\text{CF}} = \sum_{kq} B_{kq} C_q^{(k)} \tag{6}
$$

where CF Hamiltonian is given by \mathcal{H}_{CF} . SPM can be used to find the CF parameters in (6) for a metal-ligand complex [21- 22] as:

$$
B_{kq} = \sum_{i} \overline{A}_{k} \left(\frac{R_{0}}{R_{i}} \right)^{t_{k}} K_{kq} \left(\theta_{i}, \varphi_{i} \right). \tag{7}
$$

 R_0 gives the reference distance, R_i , θ_i , φ_i denote the ith ligand spherical polar coordinates and K_{kq} are the coordination factors [31]. B_{kq} (k = 2, 4; q = 0, 2, 4) [31] are obtained by using the values of \overline{A}_2 = 40, 400 cm⁻¹, t₂ = 1.3, t₄ = 3.4 and

 A_4 =11, 700 cm⁻¹. Table 3 lists the calculated B_{kq} parameters. \overline{a} For center I, the ratio $|B_{22}|/|B_{20}| = 0.880$ suggests that the B_{kq} parameters that were evaluated are standardized [30]. The total Hamiltonian is diagonalized to determine the Cr^{3+} ion's CF energy levels in KMgCST single crystals using the B_{kq} parameters found in Table 3 and the CFA computer program [32, 33]. The calculated energy values are shown in Table 4. The calculated and experimental energy values for Cr^{3+} . KZnCST with oxygen ligands are contrasted [11] as no optical absorption study of Cr^{3+} : KMgCST is reported. The theoretical and experimental energy values appear in reasonable agreement based on Table 4. Therefore, theoretical examination of Cr^{3+} ions at Mg^{2+} sites in KMgCST validates the findings of the experiment [11, 14].

Table 3. The parameters B_{kq} of Cr^{3+} for center I with distortion in a single crystal of KMgCST.

			B_{kq} (cm ⁻¹) Parameters Computed				
Site	R_o^A	B_{20}	B_{22}	B_{AB}	B_{42}	B_{xx}	1.822.4.820
Center I			WD 2.00 5724.185 5041.045 780.666 155.454 -1104.54 0.880				
		$WD = With distortion$				$\overline{}$	

The configurational-coordinate (CC) model, along with Franck-Condon analysis, now provides an explanation for the phosphors activated by Cr^{3+} and their optical absorption spectra [37]. In Cr^{3+} , the different transitions between excited states and ground states are a consequence of the lattice vibrations' strong coupling (CC model) [37]. The CC model is not being used here and so there is difference between excited-state peak energies found here and energies of the zero-phonon line (ZPL) discussed in [37, 38]. Two groups of oxide-phosphors doped with Cr^{3+} are taken up: (i) O-Cr-A type, (ii) O-Cr-B type. The luminescence properties of type (i) phosphors are found from the luminescence transitions linked with ${}^{2}E_{g}$ as the strength of their crystal fields falls in the region of $Dq/B > 2.1$ while type (ii) phosphors have a crystal-field strength lying within the range of $Dq/B < 2.1$, as a result, the optical transitions related with ${}^{4}T_{2g}$ are utilized to obtain their luminescence properties. KMgCST: Cr^{3+} falls under (i) type phosphors ($Dq/B = 2.38$ which is >2.1) [38].

6. Conclusion and Future Scope

For Cr^{3+} ions in KMgCST single crystals, to calculate the zero-field splitting (ZFS) and crystal field (CF) parameters, the superposition model (SPM) is utilized. Calculations are performed using Cr^{3+} ions at interstitial site, Mg^{2+} ion sites, and distortion models in KMgCST crystal. When distortion is taken into account in the calculation, the experimental values and the calculated traditional ZFS values for the $Cr³⁺$ ion at Mg^{2+} sites in the KMgCST single crystal are reasonably in agreement. In the KMgCST lattice, it is established that the Cr^{3+} ions will replace Mg^{2+} ion sites. The CF energy values for Cr^{3+} ions at Mg^{2+} sites calculated with the CFA package and CF parameters show a good degree of agreement with the experimental values. Therefore, the experimental analysis is validated by the theoretical results.

Table 4. Energy values obtained by computation and experimentation (center I) of Cr^{3+} in KMgCST single crystal.

Transition from $^{4}A_{2g}(F)$ state	Observed band (cm^{-1})	Calculated band (cm^{-1})
		Center I
${}^2E_g(G)$	11975	11672, 11844
${}^2T_{lg}(G)$		12083, 12397, 13083
${}^4T_{2g}(F)$	17235	15922, 16301, 16760, 16817, 17636, 18017
${}^4T_1g(F)$	24385	18085, 18778, 18832,
${}^4T_{lg}(P)$		20976, 21182, 26544 26771, 26875, 27051,
${}^2T_{1e}(aD)$ $E_e(bD)$		27067, 28460, 28683 37346, 39238, 40066 44453, 44812

 (The values of Racah parameters A, B, and C, the spin-orbit coupling constant, and the Trees correction are 0, 724, 2484, 276 and 70 cm-1, respectively)

Correlating optical and EPR data of many more ion-host systems in the future to obtain crystals for various scientific and industrial applications may be made easier with the modeling strategy taken into account in this investigation.

Acknowledgement

The CFA computer program was provided by Professor C. Rudowicz from A. Mickiewicz University in Poznan, Poland's Chemistry Faculty which the authors are appreciative of, as well as the physics department head for the departmental facilities.

Declarations:

Ethical Approval:

This study did not take place on any private or protected land, nor did it involve any research involving human or animal subjects. Corresponding locations did not require any special permissions.

Competing interests:

The authors affirm that no known conflicting financial interests or personal relationships could have influenced any of the work described in this paper.

Authors' contributions:

Vikram Singh and Maroj Bharati - completed the figure preparation, wrote the manuscript, and did calculations. Ram Kripal- concept and oversight. The manuscript has been reviewed by all authors.

Funding:

There is no funding obtained.

Availability of data and materials:

The data will be provided upon request.

References

- [1] Dinabandhu [Halder,](https://pubs.rsc.org/en/results?searchtext=Author%3ADinabandhu%20Halder) Yatrta mohan [Jana,](https://pubs.rsc.org/en/results?searchtext=Author%3AYatramohan%20Jana) Danuta [Piwowarska,](https://pubs.rsc.org/en/results?searchtext=Author%3ADanuta%20Piwowarska) Pawel [Gnutek,](https://pubs.rsc.org/en/results?searchtext=Author%3APawe%C5%82%20Gnutek) Czeslaw [Rudowicz,](https://pubs.rsc.org/en/results?searchtext=Author%3ACzes%C5%82aw%20Rudowicz) "Tailoring singleion magnet properties of coordination polymer $C_{11}H_{18}DyN_3O_9(Dy-CP)$ using the radial effective charge model (RECM) and superposition model (SPM)", *Physical Chemistry Chemical Physics.*, Vol.**26**, pp.**19947- 19959, 2024.**
- [2] Maroj Bharati, Vikram Singh, Ram Kripal, "Modeling of $Cr³⁺$ doped Cassiterite (SnO2) Single Crystals", *IgMin Res*earch, Vol.**2**, Issue**6**, pp.**484-489, 2024.**
- [3] Shish Pal Rathee, S. S. Hooda, "EPR and superposition-model analysis of zero-field splitting parameters for Mn^{2+} doped in ZnNbOF₅.6(H₂O) and CoNbOF₅.6(H₂O) single crystals", *Indian Journal of Physics*, **2024**, [https://doi.org/10.1007/s12648-024-](https://doi.org/10.1007/s12648-024-03268-3) [03268-3](https://doi.org/10.1007/s12648-024-03268-3)
- [4] Maroj Bharati, Vikram Singh, Ram Kripal, "Zero Field Splitting Parameter of Mn2+ in PMN Single Crystals", *International Journal of Engineering Technology Research and Management*, Vol.7, pp.**43-52, 2023.**
- [5] Muhammed Acikgoz, Ram Kripal, Madan Gopal Misra, Awadhesh Kumar Yadav, Pawel Gnutek, Czeslaw Rudowicz, "Theoretical analysis of crystal field parameters and zero field splitting parameters for Mn^{2+} ions in tetramethylammonium ions in tetramethylammonium tetrachlorozincate", *Polyhedron*, Vol. 235, p.116341, **2023.**
- [6] Roman Boca, Cyril Rajnak, Jan Titis, "Zero-Field Splitting in Hexacoordinate Co(II) Complexes", *Magnetochemistry*, Vol.9, pp. 100, **2023.**
- [7] Maroj Bharati, Vikram Singh, Ram Kripal, "Modeling of Mn²⁺ doped CdGa2Se⁴ single crystals", *International Journal of Engineering Inventions*, Vol.**12**, pp.**170-175, 2023.**
- [8] Ram Kripal, "Zero Field Splitting Parameter of Mn²⁺⁻Doped Tl2Cd2(SO4)³ Single Crystals at Axial Symmetry Site", *Acta Physica Polonica A,* Vol.143, pp.**217-220, 2023.**
- [9] Sangita Pandey, Ram Kripal, Awadhesh Kumar Yadav, Muhmmed Açıkg¨oz, Pawel Gnutek, Czeslaw Rudowicz,"Implications of direct conversions of crystal field parameters into zero-field splitting ones - Case study: Superposition model analysis for Cr^{3+} ions at orthorhombic sites in LiKSO4", *Journal of Luminiscence*, Vol. 230**,** p. 117548, **2021.**
- [10] Mitsuo Yamaga, Akhilesh Kumar Singh, Douglas Cameron, Pajul R. Edwards, Michal Boćkowski, ["Crystal-field analysis of](https://www.sciencedirect.com/science/article/pii/S0022231324001212) [photoluminescence from orthorhombic Eu centers and energy](https://www.sciencedirect.com/science/article/pii/S0022231324001212) [transfer from host to Eu in GaN co-doped with Mg and Eu"](https://www.sciencedirect.com/science/article/pii/S0022231324001212), *[Journal of Luminiscence.](https://www.sciencedirect.com/journal/journal-of-luminescence)*, Vol. 270, Issue 6, p.120557, **2024**.
- [11] B. Deva Prasad Raju, J. Lakshmana Rao, K.V. Narasimhulu, N. O. Gopal, C.S. Sunandana, "EPR and optical absorption studies on Cr^{3+} ions doped in KZnClSO₄.3H₂O single crystals", *Spectrochimica Acta Part A*, Vol **61**, pp.**2195–2198, 2005.**
- [12] M. A. Martin-Luengo, M.Yates, ["Zeolitic materials as catalysts for](https://link.springer.com/article/10.1007/BF01153053) [organic syntheses"](https://link.springer.com/article/10.1007/BF01153053), J*ournalof Materials Sciience,* Vol. 30, pp.**4483- 4491, 1995.**
- [13] S. N. Reddy, R. V. S. S. N. Ravikumar, B. J. Reddy, Y. P. Reddy, P. S. Rao, "Spectroscopic investigations on Fe^{3+} , Fe^{2+} and Mn2+ bearing antigorite mineral", *Neues Jahrbuch Fur Mineralogie-Monatshefte*, Vol. **6**, p.261, **2001**.
- [14] S. Dhanuskodi, A. Pricilla Jeyakumari, "EPR studies of Cr³⁺ ions in kainite single crystals", *Matials Chemistry and Physics*, Vol. 87, pp.**292–296, 2004.**
- [15] Paul D. Robinson, J. H. Fang, Y. Ohya, "The Crystal Structure of Kainite", *The American Mineralogist*, Vol. 57, pp.**1325-1332, 1972.**
- [16] Czeslaw Rudowicz, Miroslaw Karbowiak, "Disentangling Intricate Web of Interrelated Notions at the Interface Between the Physical (Crystal Field) Hamiltonians and the Effective (Spin) Hamiltonians", *Coordination Chemistry Review*, Vol.287, pp.**28-63, 2015.**
- [17] Czeslaw Rudowicz, "Concept of spin Hamiltonian, forms of zero field splitting and electronic Zeeman Hamiltonians and relations between parameters used in EPR. A critical review", *Magnetic Resonance Review*, Vol. 13**, pp.** 1-89, 1987, Erratum: Czdeslaw Rudowicz, *Magnetic Resonance Review*, Vol. 13, p. 335, **1988.**
- [18] S. I. Nikitin, E. M. Kutashova, R.V.Yusupov, R. I. Karimov, A. G. Kiiamov, ["Laser spectroscopy and crystal field analysis of](https://www.sciencedirect.com/science/article/pii/S0022231324001807) [energy level structure of Tm](https://www.sciencedirect.com/science/article/pii/S0022231324001807)³⁺ ions in SrY₂O₄ crystal" *[Journal of](https://www.sciencedirect.com/journal/journal-of-luminescence) [Luminiscence.,](https://www.sciencedirect.com/journal/journal-of-luminescence)* Vol. 272, Issue **8**, p.120616, **2024.**
- [19] Czeslaw Rudowicz, "Transformation Relations for theConventional O_k^q and NormalisedO'_k^q Stevens Operator equivalents with k=1 to 6 and -k ≤q≤ k", Journal of Physics C: Solid State Physics, Vol. 18, pp.1415-1430, 1985, Erratum: Czeslaw Rudowicz, *Journal of Physics C: Solid State Physics*, Vol. 18, p.3837, **1985**.
- [20] Czeslaw Rudowicz, C. Y. Chung, "The generalization of the extended Stevens operators to higher ranks and spins, and a systematic review of the tables of the tensor operators and their matrix elements", *Journal of Physics: Condensed Matter*, Vol.**16**, pp.**5825-5847, 2004.**
- [21] D. J. Newman, B. Ng, "Superposition model", Ch. 5 in:Newman D J, Ng B. (Eds.). "Crystal Field Handbook", *Cambridge University Press*, UK, pp. **83–119, 2000.**
- [22] D. J. Newman, B. Ng, "The Superposition model of crystal fields", *Reports of Progress in Phys*ics, Vol. 52**,** pp**. 699-763, 1989.**
- [23] Czeslaw Rudowicz, "On the Derivation of the Superposition-Model Formulae Using the Transformation Relations for the Stevens Operators", *Journal of Physics C: Solid State Physics*, Vol.**20**, pp.**6033-6037, 1987.**
- [24] Czeslaw Rudowicz, Pawel Gnutek, Muhmmed Acikgoz,"Superposition Model in Electron Magnetic Resonance Spectroscopy-A Primer for Experimentalists with Illustrative Applications and Literature Database", *Applied Spectroscopy Review*, Vol.**54**, pp.**673-718, 2019.**
- [25] Muhmmred Açıkgöz, "A study of the impurity structure for $3d³$ $(Cr^{3+}$ and Mn^{4+}) ions doped into rutile TiO₂ crystal", *Spectrochimica Acta A*, Vol. **86**, pp.**417-422**, **2012**.
- [26] K.A. Müller, W. Berlinger, J. Albers, "Paramagnetic resonance and local position of Cr^{3+} in ferroelectric BaTiO₃", *Physical Review B*, Vol. 32, pp. 5837-5850, **1985.**
- [27] K. A. Muller, W. Berlinger, "Superposition Model for Sixfold-Coordinated Cr³⁺ in Oxide Crystals (EPR Study)", *Journal of Physics C: Solid State Physics*, Vol. 16, pp.6861-6874, **1983**.
- [28] T. H. Yeom, Y. M. Chang, Czeslaw Rudowicz, S. H.Choh, "Cr³⁺ Centres in LiNbO3: Experimental and Theoretical Investigation of Spin Hamiltonian Parameters", *Solid State Communications*, Vol. 87, pp.**245-249, 1993.**
- [29] E. Siegel, K. A. Muller, "Structure of Transition-Metal-Oxygen-Vacancy Pair Centers",*Physical Review B*, Vol. 19, pp.**109-120, 1979.**
- [30] Czeslaw Rudowicz, Richard Bramley, "On standardization of the spin Hamiltonian and the ligand field Hamiltonian for orthorhombic symmetry", *Journal of Chemical Physics*, Vol. 83, pp. **5192-5197, 1985.**
- [31] Y.Y. Yeung, D. J. Newman, "Superposition-model analyses for the Cr3+ ⁴A² ground state", *Physical. Review B,* Vol.**34***,* pp.**2258-2265, 1986***.*
- [32] Y. Y. Yeung, Czeslaw Rudowicz, "Ligand Field Analysis of the $3d^N$ Ions at Orthorhombic or Higher Symmetry Sites", *Computers and Chemistry*, Vol.**16**, pp.**207-216, 1992.**
- [33] Y. Y. Yeung, Czeslaw Rudowicz, "Crystal Field Energy Levels and State Vectors for the $3d^N$ Ions at Orthorhombic or Higher Symmetry Sites", *Journal of Computational Physics*, Vol.**109**, pp.**150-152, 1993.**
- [34] Y. M. Chang, Czeslaw Rudowicz, Y.Y.Yeung, "Crystal field analysis of the $3d^N$ ions at low symmetry sites including the 'imaginary' terms", *Computers in Physics*, Vol. 8, pp.**583-588, 1994.**
- [35] B. G. Wybourne, "Spectroscopic Properties of Rare Earth", Wiley, New York, USA, 1965.
- [36] B. N. Figgis, M.A. Hitchman, "Ligand Field Theory and its Applications", *Wiley*, New York, USA, **2000.**
- [37] Sadao Adachi, "Photoluminescence Spectroscopy and Crystal-Field Parameters of Cr³⁺ Ion in Red and Deep Red-Emitting Phosphors", *ECS Journal of Solid State Science and Tech*nology, Vol.8, pp.**R164-R168**, **2019.**
- [38] Sadao Adachi, "Review—Photoluminescence Properties of Cr³⁺-Activated Oxide Phosphors", *ECS Journal of Solid State Science and Technology*, Vol. 10, p. 026001, **2021.**

AUTHORS PROFILE

Maroj Bharati did M.Sc. in Physics from University of Allahabad in 2019. She is pursuing Ph. D. from NGB DU, Allahabad on the topic 'EPR Study of Transition Ion doped Single Crystals-Superposition Model Analysis'. She has authored several research papers in reputable international journals on her subject.

Dr. Vikram Singh is working as Assistant Professor at physics Department of Nehru Gram Bharti Deemed to be University, Allahabad. He works in Quantum Optics, Non Linear Optics, EPR and Nano Composites. His research papers have been published in several reputable international journals which have been cited by several other workers.

research laboratory includes Varian X-band(9.5 GHz) CW(continuous wave) EPR spectrometer operational in the 77-1000K temperature range and Unicam 5636 UV/Visible spectrophotometer operating in the wavelength range 195- 1100 nm. He collaborates actively with researchers at NPL (National Physical Laboratory), New Delhi, India and with Prof. C. Rudowicz, Faculty of Chemistry, A. Mikowicz. University, Poznan, Poland. In addition to polycrystalline and single crystal CW EPR he does optical absorption in the wavelength range mentioned above. He is also engaged in EPR research of nano-materials. 20 Ph.D. students have received their degrees under his supervision. He has acted as an external examiner to several Ph.D. and M. Phil. theses examinations outside AllahabadUniversity. He serves as a referee to important journals in physical sciences which publish EPR research (J. Phys. Chem. Solids, Solid State Commun., J. Magn. Magn Material, Spectrochim. Acta, J. Mat. Sci., J. Alloys and Comp., Chem. Phys., Chem. Phys. Lett., Phys. Scripta, J. Magn. Reson., Indian J. Phys.). He has published several articles in EPR and has written a book on Practical Physics, Introduction to Electromagnetic Theory. His research has been continuously supported by UGC (University Grants Commission), CSIR (Council of Scientific and Industrial Research), DST (Department of Science and Technology) and CST (Council of Science and Technology), India